

2. Referring to Eq. 22-6, we use the binomial expansion (see Appendix E) but keeping higher order terms than are shown in Eq. 22-7:

$$\begin{aligned} E &= \frac{q}{4\pi\epsilon_0 z^2} \left( \left( 1 + \frac{d}{z} + \frac{3}{4} \frac{d^2}{z^2} + \frac{1}{2} \frac{d^3}{z^3} + \dots \right) - \left( 1 - \frac{d}{z} + \frac{3}{4} \frac{d^2}{z^2} - \frac{1}{2} \frac{d^3}{z^3} + \dots \right) \right) \\ &= \frac{q d}{2\pi\epsilon_0 z^3} + \frac{q d^3}{4\pi\epsilon_0 z^5} + \dots \end{aligned}$$

Therefore, in the terminology of the problem,  $E_{\text{next}} = q d^3 / 4\pi\epsilon_0 z^5$ .

3. Our system is a uniformly charged disk of radius  $R$ . We compare the field strengths at different points on its axis of symmetry. At a point on the axis of a uniformly charged disk a distance  $z$  above the center of the disk, the magnitude of the electric field is given by Eq. 22-26:

$$E = \frac{\sigma}{2\epsilon_0} \left[ 1 - \frac{z}{\sqrt{z^2 + R^2}} \right]$$

where  $R$  is the radius of the disk and  $\sigma$  is the surface charge density on the disk. The magnitude of the field at the center of the disk ( $z = 0$ ) is  $E_c = \sigma/2\epsilon_0$ . We want to solve for the value of  $z$  such that  $E/E_c = 1/4$ . This means

$$1 - \frac{z}{\sqrt{z^2 + R^2}} = \frac{1}{4} \Rightarrow \frac{z}{\sqrt{z^2 + R^2}} = \frac{3}{4}.$$

Squaring both sides, then multiplying them by  $z^2 + R^2$ , we obtain  $16z^2 = 9(z^2 + R^2)$ . Thus,  $z^2 = 9R^2/7$ , or  $z = 3R/\sqrt{7}$ . With  $R = 0.600$  m, we have  $z = 0.680$  m.

11. From symmetry, we see that the net field at  $P$  is twice the field caused by the upper semicircular charge  $+q = \lambda(\pi R)$  (and that it points downward). Adapting the steps leading to Eq. 22-21, we find

$$\vec{E}_{\text{net}} = 2(-\hat{j}) \frac{\lambda}{4\pi\epsilon_0 R} \sin\theta \Big|_{-90^\circ}^{90^\circ} = -\left(\frac{q}{\epsilon_0\pi^2 R^2}\right)\hat{j}.$$

(a) With  $R = 4.25 \times 10^{-2} \text{ m}$  and  $q = 1.50 \times 10^{-11} \text{ C}$ , we obtain

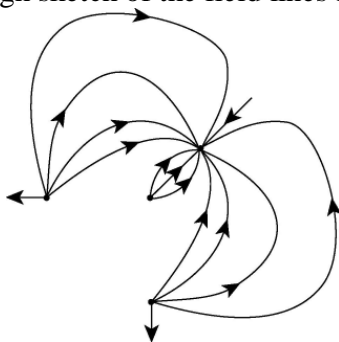
$$|\vec{E}_{\text{net}}| = \frac{q}{\epsilon_0\pi^2 R^2} = \frac{1.50 \times 10^{-11} \text{ C}}{(8.85 \times 10^{-12} \text{ C}^2/\text{N} \cdot \text{m}^2)\pi^2(4.25 \times 10^{-2} \text{ m})^2} = 95.1 \text{ N/C}.$$

(b) The net electric field  $\vec{E}_{\text{net}}$  points in the  $-\hat{j}$  direction, or  $-90^\circ$  counterclockwise from the  $+x$  axis.

32. We place the origin of our coordinate system at point  $P$  and orient our  $y$  axis in the direction of the  $q_4 = -12q$  charge (passing through the  $q_3 = +3q$  charge). The  $x$  axis is perpendicular to the  $y$  axis, and thus passes through the identical  $q_1 = q_2 = +5q$  charges. The individual magnitudes  $|\vec{E}_1|$ ,  $|\vec{E}_2|$ ,  $|\vec{E}_3|$ , and  $|\vec{E}_4|$  are figured from Eq. 22-3, where the absolute value signs for  $q_1$ ,  $q_2$ , and  $q_3$  are unnecessary since those charges are positive (assuming  $q > 0$ ). We note that the contribution from  $q_1$  cancels that of  $q_2$  (that is,  $|\vec{E}_1| = |\vec{E}_2|$ ), and the net field (if there is any) should be along the  $y$  axis, with magnitude equal to

$$\vec{E}_{\text{net}} = \frac{1}{4\pi\epsilon_0} \left( \frac{|q_4|}{(2d)^2} - \frac{q_3}{d^2} \right) \hat{j} = \frac{1}{4\pi\epsilon_0} \left( \frac{12q}{4d^2} - \frac{3q}{d^2} \right) \hat{j}$$

which is seen to be zero. A rough sketch of the field lines is shown below:



50. Due to the fact that the electron is negatively charged, then (as a consequence of Eq. 22-28 and Newton's second law) the field  $\vec{E}$  pointing in the  $+y$  direction (which we will call "upward") leads to a downward acceleration. This is exactly like a projectile motion problem as treated in Chapter 4 (but with  $g$  replaced with  $a = eE/m = 8.78 \times 10^{11} \text{ m/s}^2$ ). Thus, Eq. 4-21 gives

$$t = \frac{x}{v_0 \cos \theta_0} = \frac{3.00 \text{ m}}{(4.00 \times 10^6 \text{ m/s}) \cos 40.0^\circ} = 9.80 \times 10^{-7} \text{ s}.$$

This leads (using Eq. 4-23) to

$$\begin{aligned} v_y &= v_0 \sin \theta_0 - at = (4.00 \times 10^6 \text{ m/s}) \sin 40.0^\circ - (8.78 \times 10^{11} \text{ m/s}^2)(9.80 \times 10^{-7} \text{ s}) \\ &= 1.71 \times 10^6 \text{ m/s}. \end{aligned}$$

Since the  $x$  component of velocity does not change, then the final velocity is

$$\vec{v} = (3.06 \times 10^6 \text{ m/s}) \hat{i} + (1.71 \times 10^6 \text{ m/s}) \hat{j}.$$

59. (a) The smallest arc is of length  $L_1 = \pi r_1 / 2 = \pi R / 2$ ; the middle-sized arc has length  $L_2 = \pi r_2 / 2 = \pi(2R) / 2 = \pi R$ ; and, the largest arc has  $L_3 = \pi(3R) / 2$ . The charge per unit length for each arc is  $\lambda = q / L$  where each charge  $q$  is specified in the figure. Thus, we find the net electric field to be

$$E_{\text{net}} = \frac{\lambda_1(2 \sin 45^\circ)}{4\pi\epsilon_0 r_1} + \frac{\lambda_2(2 \sin 45^\circ)}{4\pi\epsilon_0 r_2} + \frac{\lambda_3(2 \sin 45^\circ)}{4\pi\epsilon_0 r_3} = \frac{4Q}{\sqrt{2}\pi(4\pi\epsilon_0)R^2}$$

$$= \frac{4(8.99 \times 10^9 \text{ N} \cdot \text{m}^2 / \text{C}^2)(4.00 \times 10^{-6} \text{ C})}{\sqrt{2}\pi(0.050 \text{ m})^2} = 1.30 \times 10^7 \text{ N/C}$$

(b) The direction is  $-45^\circ$ , measured counterclockwise from the  $+x$  axis.