

3. (a) The current in each strand is $i = 0.750 \text{ A}/63 = 1.19 \times 10^{-2} \text{ A} = 11.9 \text{ mA}$.
- (b) The potential difference is $V = iR = (1.19 \times 10^{-2} \text{ A})(2.65 \times 10^{-6} \Omega) = 3.15 \times 10^{-8} \text{ V}$.
- (c) The resistance is $R_{\text{total}} = (2.65 \times 10^{-6} \Omega)/63 = 4.21 \times 10^{-8} \Omega$.

15. (a) From $P = V^2/R = AV^2 / \rho L$, we solve for the cross-sectional area:

$$A = \frac{\rho LP}{V^2} = \frac{(5.00 \times 10^{-7} \text{ } \Omega \cdot \text{m})(5.85 \text{ m})(4000 \text{ W})}{(112 \text{ V})^2} = 9.33 \times 10^{-7} \text{ m}^2.$$

(b) Since $L \propto V^2$ the new length should be

$$L' = L \left(\frac{V'}{V} \right)^2 = (5.85 \text{ m}) \left(\frac{100 \text{ V}}{112 \text{ V}} \right)^2 = 4.66 \text{ m}.$$

36. Since the potential difference V and current i are related by $V = iR$, where R is the resistance of the electrician, the fatal voltage is $V = (50 \times 10^{-3} \text{ A})(2100 \ \Omega) = 105 \text{ V}$.

45. (a) The current resulting from this non-uniform current density is

$$i = \int_{\text{cylinder}} J_a dA = \frac{J_0}{R} \int_0^R r \cdot 2\pi r dr = \frac{2}{3} \pi R^2 J_0 = \frac{2}{3} \pi (2.67 \times 10^{-3} \text{ m})^2 (5.50 \times 10^4 \text{ A/m}^2) \\ = 0.821 \text{ A}.$$

(b) In this case, we have

$$i = \int_{\text{cylinder}} J_b dA = \int_0^R J_0 \left(1 - \frac{r}{R}\right) 2\pi r dr = \frac{1}{3} \pi R^2 J_0 = \frac{1}{3} \pi (2.67 \times 10^{-3} \text{ m})^2 (5.50 \times 10^4 \text{ A/m}^2) \\ = 0.411 \text{ A}.$$

(c) The result is different from that in part (a) because J_b is higher near the center of the cylinder (where the area is smaller for the same radial interval) and lower outward, resulting in a lower average current density over the cross section and consequently a lower current than that in part (a). So, J_a has its maximum value near the surface of the wire.

48. (a) Since the material is the same, the resistivity ρ is the same, which implies (by Eq. 26-11) that the electric fields (in the various rods) are directly proportional to their current-densities. Thus, $J_1: J_2: J_3$ are in the ratio 2.5/4/1.5 (see Fig. 26-27). Now the currents in the rods must be the same (they are “in series”) so

$$J_1 A_1 = J_3 A_3, \quad J_2 A_2 = J_3 A_3 .$$

Since $A = \pi r^2$, this leads (in view of the aforementioned ratios) to

$$4r_2^2 = 1.5r_3^2, \quad 2.5r_1^2 = 1.5r_3^2 .$$

Thus, with $r_3 = 1.70$ mm, the latter relation leads to $r_1 = (1.5/2.5)^{1/2}(1.70 \text{ mm}) = 1.32$ mm.

(b) The $4r_2^2 = 1.5r_3^2$ relation leads to $r_2 = (1.5/4.0)^{1/2}(1.70 \text{ mm}) = 1.04$ mm.